1. Introduction

Nowadays, different topologies of power electronics-based custom power devices are available due to the launch of active power filters to reduce the power quality (PQ) issues in three-phase power utility networks (PUN) (Bayu, 2020; Mangaraj and Sabat, 2021). In recent years, the integration of shunt compensators with low and medium voltage PUN has gained significant popularity (Bayu, 2020; Sabat et al., 2021). Clients ranging from domestic to industrial are demanding the utility companies to enhance the quality of power delivered. Power electronics devices integrated with unbalanced reactive loads generate PQ problems introducing source currents that are ‘distorted and unbalanced’ (Mangaraj and Sabat, 2021; Patel and Makwana, 2021). Generally, capacitor banks and passive filters are employed to enhance the PQ in PUN. But, some demerits have been observed in these devices such as system parameters being dependent on performance, resonance with line reactance and compensation limit (Bayu, 2020).

The conventional two-level voltage source inverter (VSI) is frequently used as a common device to transfer the generated energy from the energy source to the PUN (Mangaraj and Sabat, 2021; Ray et al., 2017). But an additional power stage conversion is required because VSI is a buck converter, which increases the cost and decreases the efficiency of the overall system (Reddivari and Jena, 2021). The above negative aspects of VSI decreases its reliability and flexibility. To overcome the limitations of the VSI, an impedance source inverter (ZSI) is developed (Roomi, 2019). It performs both buck/boost functions (Liang Cheng, 2018; Roomi, 2019). The configuration of ZSI consists of an impedance network (X-shaped), which use two inductors and two capacitors. The advantages of ZSI are its ability to supply higher AC voltage compared to VSI and protecting the inverter bridge from open and short circuits (Chauan et al., 2018; Liang Cheng, 2018; Roomi, 2019). But ZSI also has some disadvantages such as...
more stress on the capacitors, low boost factor and discontinuous input current. To overcome the disadvantages of ZSI, a Quasi Z-source inverter (QZSI) is suggested because it can absorb constant power from the input side (Mohammadi et al., 2018). It consists of two capacitors, two inductors, a DC source and a diode (Bayhan et al., 2016). The operation of QZSI comprises of two states. During state-1 (active state), it operates as a conventional VSI but during state-2 (shoot-through state), two switches of one leg of the inverter are switched ON simultaneously. Most significantly, shoot-through (state-2 operation) is allowed in the QZSI, whereby the upper and lower switches of each inverter leg can be switched on at the same time, which eliminates dead-time to reduce output waveform distortion (Bhavan et al., 2016; Battiston et al., 2016; Gu et al., 2018; Mohammadi et al., 2018).

In recent years, back to back connected configuration with common self-supported capacitors received more attention due to its ability to provide continuous input current and reduced component stress in the impedance network (Friedli et al., 2012; Mahato et al., 2020; Tang et al., 2015; Zhou et al., 2016). Also, the back to back connected QZSIs (BB-QZSI) topology has attained the ability to mitigate the PQ issues as per the recommended standard grid code (Car et al., 2021). Hence, it is introduced as a new segment in low- and medium-voltage PUN.

A distribution static compensator (DSTATCOM) is a shunt compensator, which uses force commutated power electronics insulated gate bipolar transistors (IGBT) to improve PQ and control power flow. Also, it is a fast-acting device that regulates the voltage at the point of common coupling (PCC) by absorbing or providing reactive current (Mangaraj and Sabat, 2021 and Sabat and Mangaraj, 2021). The $\text{icos}\phi$ control scheme permits a smooth transition from the steady-state operation into the unbalanced operation of a three-phase PUN while suppressing the PQ issues (Mangaraj et al., 2020; Mangaraj et al., 2020). The significant features of the control technique are listed as follows:

- Simple and error-free computation to extract the active and reactive parts of the fundamental load current (Mangaraj et al., 2020; Mangaraj and Sabat, 2021).
- Toughness, tracking and adaptive abilities are the initial findings of this control algorithm (Mangaraj and Sabat, 2021).
- Better source current shaping, switching stress reduction, dc-link voltage reduction, improvement in voltage regulation and three-phase balance voltage obtained at the PCC of PUN (Mangaraj et al., 2020).

The original contribution of the BB-QZSI-based DSTATCOM topology is as follows:

- To the best of the author’s knowledge, the shunt compensation of the BB-QZSI under PQ issues using $\text{icos}\phi$ control algorithm has not been investigated before this research work.
- The connected total nonlinear load current is divided by QZSI-1 and QZSI-2. Hence, it reduces the failure percentage of IGBT. When one QZSI shuts down, the other can continue the operation. Hence, it decreases the energy lost and downtime cost and ultimately reliability is increased.
- The simulation results highlight the performance of shunt compensation and the results obtained from BB-QZSI are better as compared to QZSI.
- The significant contributions of BB-QZSI are identified and they are reduced switching stress, balanced voltage at PCC, power factor (PF) correction, source current shaping, etc.

In this article, the circuit description with the operation of the BB-QZSI is presented in Section 2. The $\text{icos}\phi$ control technique is presented in Section 3 and applied to QZSI integrated DSTATCOM. Section 4 describes the simulation performance of the topologies by showing the effectiveness of the DSTATCOM. Section 5 concludes the paper by pointing to the salient features and the performance of BB-QZSI over QZSI.

2. PUN Operation And Design Of BB-QZSI-Based DSTATCOM

A dynamical three phase three wire PUN with BB-QZSI-based DSTATCOM, one non-linear load and three-phase balance sources which complete the utility network is depicted in Figure 1. PCC is a suitable point where the PUN, non-linear load and shunt compensator are connected together. Also, it is a convenient point to transfer the electric power between the load and PUN. In Figure 1, the three-phase supply, current sensitive three-phase non-linear load (diode bridge rectifier with resistor ‘R’ and inductor ‘L’) and BB-QZSI-based DSTATCOM are connected at the PCC of PUN. The non-linear load draws three-phase load currents $(i_{la}, i_{lb}, i_{lc})$ from the three-phase balanced supply voltage $(v_a, v_b, v_c)$. The PUN supplies the source currents $(i_{sa}, i_{sb}, i_{sc})$ to the connected load interfacing the distribution line impedance $Z_s'$. The BB-QZSI topology consists of two back to back connected QZSIs represented in Figure 1 as QZSI-1 and QZSI-2. A self-supported capacitor ‘C’ is connected to the input side of BBC-QZSI-based DSTATCOM.
as shown in Figure 1. Both QZSI-1 and QZSI-2 are supplied from a common dc-link voltage ($V_{dc}$). The BBC-VSI-based DSTATCOM supplies the compensating currents ($i_{ca}, i_{cb}, i_{cc}$) from QZSI-1 and ($i'_{ca}, i'_{cb}, i'_{cc}$) from QZSI-2.

A single self-supported capacitor supports both QZSIs to reduce the PQ issues. Each QZSI is constructed having three legs (two switches in each leg). Hence, a total of six switches are used. It attains $2^6$ or 64 switching combinations during DSTATCOM operation. Figure 2 represents the QZSI configuration which consists of two capacitors, two inductors, a DC source and a diode. Generally, IGBTs are preferred for high voltage, high current and low switching frequency circuits. In IGBT, a transistor is shunted by a flyback diode to conduct current in the opposite direction because reverse current flow is required in bridge circuits. Also, when a load is disconnected, the inductive load current produces high voltage peaks which requires a suitable path otherwise it will destroy the switch.
The QZSI configuration consists of two capacitors, two inductors, a DC source and a diode. The Z-network of the QZSI offers several advantages such as the ability to handle wide input voltage, constant DC from source and lower component ratings. Analysing the QZSI configuration during both non-shoot and shoot through states, different parameters are calculated. The shoot-through state and non-shoot through states of QZSI are depicted in Figure 3a and b, respectively.

Note that, $T = \text{switching period}$, $T_0 = \text{time period during shoot through state}$, $T_1 = \text{time period during non-shoot through state}$ and

$$ T = T_0 + T_1 $$

and

$$ D = \frac{T_0}{T}, \text{ where } D = \text{duty cycle}$$

Applying Kirchhoff’s voltage and current laws in Figure 3a, we have

$$ L_1 \frac{di_1}{dt} = V_{dc} - V_{c1}, $$

$$ L_2 \frac{di_2}{dt} = -V_{c2}, $$

$$ C_1 \frac{dV_{c1}}{dt} = i_1 - i_{PN} - i_{c1}, $$

$$ C_2 \frac{dV_{c2}}{dt} = i_2 - i_{PN} - i_{c2}. $$

Similarly, applying Kirchhoff’s voltage and current laws in Figure 3b, we get

$$ L_1 \frac{di_1}{dt} = V_{dc} + V_{c2}, $$

$$ L_2 \frac{di_2}{dt} = V_{c1}. $$
The instantaneous voltage and current equations are given by

\[ V_{c1} = \frac{1-D}{(1-2D)} V_{dc}, \]  
\[ V_{c2} = \frac{D}{(1-2D)} V_{dc}, \]  
\[ i_{11} = \frac{D i_{c2} + (1-D) i_{c3} + (1-D) i_{PN}}{1-2D}, \]  
\[ i_{12} = \frac{D i_{c4} + (1-D) i_{c2} + (1-D) i_{PN}}{1-2D}. \]

\( V_{PN} \) = Maximum dc-link voltage and the corresponding parameters are found by the following equations

\[ V_{PN} = V_{c1} + V_{c2}, \]  
\[ i_{12} - i_{11} = i_{c1} + i_{c2}, \]  
\[ P_{dc} = i_{dc} V_{dc}, \]  
\[ P_{c1} = i_{c1} V_{c1}, \]  
\[ P_{c2} = i_{c2} V_{c2}. \]

Gate signals for switches of QZSI are estimated by using the \( i_c \cos \phi \) control algorithm.

2.1. Design of parameters \( V_{dc}, C \) and \( L \)

The \( V_{dc} \) across the self-supported capacitor of BB-QZSI is taken as 1.6 times the peak of phase voltage (Battiston et al., 2016). Rating of the capacitor depends upon the variation of \( V_{dc} \). The maximum energy exchanged by the BB-QZSI during the transient period is equal to the change in the capacitor’s stored energy.

Note that the energy exchanged by the BB-QZSI during transient period = \( nST \) and the energy stored by the capacitor = \( \frac{1}{2} CV^2 \) (\( n \) = No. of cycles taken by the controller, \( S \) is the rating of the load in kVA and \( T \) is the system period).

\[ nST = \frac{1}{2} CV^2 \]  
\[ \text{since } V^2 = \left( V_{dc\, \text{ref}}^2 - V_{dc\, \text{allowed}}^2 \right). \]

where, \( V_{dc\, \text{ref}} \) and \( V_{dc\, \text{allowed}} \) are the reference dc voltage and maximum permissible dc voltage across capacitor during transient period, respectively.
Putting Eq. (21) in Eq. (20), we get

\[
n_{ST} = \frac{1}{2} C \left( V_{dc\, ref}^2 - V_{dc\, allowed}^2 \right)
\]

or,

\[
\frac{1}{2} C \left( V_{dc\, ref}^2 - V_{dc\, allowed}^2 \right) = n_{ST}
\]

where \( V_{dc\, allowed} = 0.8 \times V_{dc\, ref} \)

(22)

The magnitude of interfacing inductance \( L \) is calculated using the following equation

\[
L = \frac{1.6 V_m}{4 h_s f_{\text{max}}}
\]

(23)

(where, \( h_s \) = hysteresis band = 0.5 and \( f_{\text{max}} \) = Maximum switching frequency).

3. \( \text{icos}\phi \) Control Algorithm

The control structure of the \( \text{icos}\phi \) technique is presented in Figure 4. The proposed system circuit diagram of the PUN and BB-QZSI-based DSTATCOM is depicted in Figure 1. The control technique for the shunt compensator

![Fig. 4. System block diagram of \( \text{icos}\phi \) control technique. PF, power factor; QZSI, Quasi Z-source inverter.](image-url)
generates the reference compensation currents to be supplied by the DSTATCOM at the PCC of PUN. The error-free minimum calculation steps choose the response time of the DSTATCOM. The control technique has the ability to mitigate the PQ issues like reduction in source current distortion, improvement in voltage regulation, balanced voltage at PCC and improvement in PF under both balanced and unbalanced loading conditions. In shunt compensation, the supply is supposed to supply the load current’s active portion, here ‘i’ stands for the magnitude of the fundamental load current and \( \cos \phi \) is the displacement PF of the connected load. Hence, it is named as \( \cos \phi \) control algorithm. The \( \cos \phi \) controller is used to generate the gate signals for switches of inverter and the selection of this technique is due to its fast and robust dynamic response to both steady-state and transient response (Mangaraj and Sabat, 2020a, b; Singh and Bhuvaneswari, 2020).

Three steps are involved in generating the gate signals for controlling the DSTATCOM:

- Fundamental quantities of the three-phase load current are computed using the Fourier block.
- The control technique is used to generate both active and reactive parts of the load current.
- The reference source current and actual source current are given to the hysteresis current controller (HCC) to generate the switching pulses for the switches of the BB-QZSI.

The active component of fundamental load current can be computed using the below equation

\[
\begin{bmatrix}
i_{ap} \\
i_{bp} \\
i_{cp}
\end{bmatrix} = \begin{bmatrix}
\text{Re}(i_a) \\
\text{Re}(i_b) \\
\text{Re}(i_c)
\end{bmatrix} = \begin{bmatrix}
i_{a}\cos\phi_a \\
i_{b}\cos\phi_b \\
i_{c}\cos\phi_c
\end{bmatrix}.
\]  

(24)

where, \( i_{ap} \) = amplitude of the active power component of load currents, \( \text{Re}(i_a) \) = Real part of the load currents, \( i_{a}\cos\phi_a \) = amplitude of load currents multiplies with the corresponding phase cosine of the phase angle and ‘x’ stands for phases a, b and c.

The magnitude of the 'w_p' (weighted active component of fundamental load currents average) can be expressed as

\[
w_p = \left(\frac{i_{a}\cos\phi_a + i_{b}\cos\phi_b + i_{c}\cos\phi_c}{3}\right).
\]  

(25)

In the same way, the reactive power component can be expressed as

\[
\begin{bmatrix}
i_{aq} \\
i_{bq} \\
i_{cq}
\end{bmatrix} = \begin{bmatrix}
\text{Im}(i_a) \\
\text{Im}(i_b) \\
\text{Im}(i_c)
\end{bmatrix} = \begin{bmatrix}
i_{a}\sin\phi_a \\
i_{b}\sin\phi_b \\
i_{c}\sin\phi_c
\end{bmatrix}.
\]  

(26)

The weighted average value of the reactive power component \( w_q \) is given as

\[
w_q = \left(\frac{i_{a}\sin\phi_a + i_{b}\sin\phi_b + i_{c}\sin\phi_c}{3}\right).
\]  

(27)

The proportional integral (PI) controller output is expressed as

\[
w_{dp} = k_{pdp}v_{dc} + k_{idp}\int v_{dc}dt,
\]  

(28)

where, \( w_{dp} \) = total active components of the reference source currents, \( k_{pdp} \) = proportional controller, \( k_{idp} \) = integral controller and \( v_{dc} \) = error in dc voltage.

The total active components of the reference source currents are given as

\[
w_{sp} = w_{dp} + w_{lp}.
\]  

(29)
In the same manner, the total reactive components can be computed from

$$w_{sq} = w_{qq} - w_{lq}. \quad (30)$$

A 20 Hz cut-off frequency low-pass filter (LPF) is utilized for filtering of load current ripple.

The instantaneous value of the active source currents $i_{sp}$, can be computed from

$$\begin{bmatrix} i_{sap} \\ i_{sbp} \\ i_{scp} \end{bmatrix} = w_{sp} \begin{bmatrix} u_{ap} \\ u_{bp} \\ u_{cp} \end{bmatrix} \quad (31)$$

The instantaneous value of the reactive source currents $i_{sq}$, can be computed from

$$\begin{bmatrix} i_{saq} \\ i_{sbq} \\ i_{scq} \end{bmatrix} = w_{sq} \begin{bmatrix} u_{aq} \\ u_{bq} \\ u_{cq} \end{bmatrix} \quad (32)$$

Finally, the reference source currents can be estimated from

$$\begin{bmatrix} i_{sa} \\ i_{sb} \\ i_{sc} \end{bmatrix} = \begin{bmatrix} i_{sap} \\ i_{sbp} \\ i_{scp} \end{bmatrix} + \begin{bmatrix} i_{saq} \\ i_{sbq} \\ i_{scq} \end{bmatrix} \quad (33)$$

The reference source currents ($i_{sa}^*, i_{sb}^*$, and $i_{sc}^*$) and the actual source currents ($i_{sa}$, $i_{sb}$, and $i_{sc}$) of each phase are compared, and then the current error signals are supplied to HCC. It operates as, when $i_{sa} < i_{sa}^*$, switch 1 is ON and switch 4 is OFF, similarly when $i_{sa} > i_{sa}^*$, switch 1 is OFF and switch 4 is ON.

**4. Simulation Results**

The proposed $i\cos\phi$ control strategy is first simulated by using MATLAB software. At the start, the PUN is verified by connecting a current sensitive non-linear load, and the compensator is not connected at PCC. At this time, the distortion in source current is identical to the load current. The simulation model of the proposed PUN with BB-QZSI-based DSTATCOM is presented in Figure 5. Simulation results of BB-QZSI and single QZSI supported DSTATCOM using Sim power toolbox is designed and their outputs are presented in the following subsection:

**4.1. Simulation results of QZSI integrated DSTATCOM under both steady-state and dynamic states**

As shown in Figure 1, the proposed system is designed using MATLAB/Simulink. It consists of a balanced three-phase supply, current sensitive three-phase non-linear load (diode bridge rectifier with resistor $R=10 \Omega$ and inductor $L=20$ mH) and QZSI-based DSTATCOM. Here, the fundamental frequency and reference dc-link voltage of QZSI are 50 Hz and 600 V, respectively. The different important parameters of the designed system are provided in Table 1.

The QZSI current tracking characteristics under balanced and unbalanced loading conditions are depicted in Figure 6. The duration from 0.55 s to 0.6 s and 0.7 s to 0.75 s shows the balanced loading condition but the duration from 0.6 s to 0.7 s is considered for unbalanced loading condition. The QZSI dc-link voltage $v_{dc}$ (ref) is varied from 700 V to 770 V during the unbalanced condition. Figure 7a and b represents the Fast Fourier Transform FFT analysis of source current and sensitive load current, respectively. But the Figure 7c and d waveforms represent the phase displacement of supply voltage and current before and after compensation, respectively. After compensation, the source current’s total harmonic distortion (THD) is reduced to 4.66% and an improvement in PF 0.971 is found.
4.2. Simulation results of BB-QZSI integrated DSTATCOM under both steady-state and dynamic state

The same parameters are used to build the proposed topology; instead of a single QZSI, dual QZSIs are connected back-to-back here. The dynamic and transient responses of BB-QZSI current tracking characteristics are depicted in Figure 8.

The duration of 0.55 s to 0.6 s and 0.7 s to 0.75 s shows the balanced loading condition but the duration from 0.6 s to 0.7 s is considered for unbalanced loading condition. Here, the reference dc-link voltage is varied from 600 V to 680 V during the unbalanced condition. After compensation, the source current THD% is reduced to 3.21% which is depicted in Figure 9a. The load current THD 29.75% is shown in Figure 9b. The phase displacements between the corresponding source voltage and current before and after compensation are depicted in Figure 9c and d, respectively.

Source current THD reduction must be taken into account to compare these two DSTATCOMs, this reduction in THD of PUN leads to a better performance of DSTATCOM and an increase in reliable and flexible operation.

### Table 1. Different parameters of the simulation study

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Detail</th>
<th>Magnitude</th>
</tr>
</thead>
<tbody>
<tr>
<td>$v_{dc}$</td>
<td>dc-link voltage</td>
<td>600 V</td>
</tr>
<tr>
<td>$C_{dc}$</td>
<td>Capacitor</td>
<td>2,000 µF</td>
</tr>
<tr>
<td>$k_{pDp}$</td>
<td>Proportional controller gain</td>
<td>0.01</td>
</tr>
<tr>
<td>$k_{idp}$</td>
<td>Integral controller gain</td>
<td>0.05</td>
</tr>
<tr>
<td>$R_c$</td>
<td>Compensator resistance</td>
<td>0.25 Ω</td>
</tr>
<tr>
<td>$L_c$</td>
<td>Compensator inductance</td>
<td>1.5 mH</td>
</tr>
<tr>
<td>$R_s$</td>
<td>Source resistance</td>
<td>0.5 Ω</td>
</tr>
<tr>
<td>$L_s$</td>
<td>Source inductance</td>
<td>2 mH</td>
</tr>
<tr>
<td>$v_s$</td>
<td>Nominal supply voltage</td>
<td>230 V/phase</td>
</tr>
<tr>
<td>$f_s$</td>
<td>Nominal fundamental frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td>$K_{pr}$</td>
<td>Controller (AC proportional)</td>
<td>0.2</td>
</tr>
<tr>
<td>$K_{ir}$</td>
<td>Controller (AC integral)</td>
<td>1.1</td>
</tr>
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</table>
Fig. 6. Simulation waveform of three-phase supply voltage, three-phase supply current, three-phase load current, three-phase compensating current and QZSI dc-link voltage. QZSI, Quasi Z-source inverter.

Fig. 7. Simulation results of QZSI, (a) spectrum analysis of source current after compensation $i_s$ THD%, (b) spectrum analysis of load current after compensation $i_l$ THD%, (c) before compensation phase displacement between the source voltage and source current and (d) after compensation phase displacement between the source voltage and source current (QZSI, Quasi Z-source inverter; THD, total harmonic distortion).
Fig. 8. Simulation waveform of three-phase supply voltage, three-phase supply current, three-phase load current, three-phase compensating current and QZSI dc-link voltage. QZSI, Quasi Z-source inverter.

Fig. 9. Simulation results of BB-QZSI, (a) spectrum analysis of source current after compensation i_s THD%, (b) spectrum analysis of load current after compensation i_l THD%, (c) before compensation phase displacement between the source voltage and source current and (d) after compensation phase displacement between the source voltage and source current. BB-QZSI, back to back connected QZSIs. QZSI, Quasi Z-source inverter; THD, total harmonic distortion.
The performance parameters of single and BB-QZSI are shown in Table 2. The performance of BB-QZSI-based DSTATCOM under PQ issues with relevant similar work ‘A High-Performance Microgrid With a Mechanical SensorlessSynRG Operated Wind Energy Generating System’ using back-to-back VSI configuration with a common dc-link is arranged in Table 3 (Zhou et al., 2016).

### 5. Conclusion

This work concludes that BB-QZSI with $icos$ control strategy for PUN applications meets the demand of buck/boost single-stage conversion and reactive power compensation. It has the ability to get a better PQ and stability of PUN. Moreover, an inclusive evaluation between classic QZSI and BB-QZSI-based DSTATCOM has been projected to provide shunt compensation. Although both topologies-based DSTATCOM schemes differ in the THD reduction, still, it has been found that the BB-QZSI topology can efficiently eliminate source-side harmonic reduction, minimize switching losses, voltage balancing at PCC, PF improvement, and reasonable voltage regulation with system stability. Furthermore, it is shown that the BB-QZSI has good shunt compensation capability and can reduce the THD well below the limit of the grid code over QZSI. Based on the analysis made from theoretical propositions and simulated results, a typical BB-QZSI is finally suggested.

### References


